# 7-4

#### Puzzle: Letter Scramble

#### Properties of Logarithms

Next to each expression in the left column, write the letter of the expression in the right column whose value is equivalent to it. Some letters will be used more than once. Unscramble the letters to find the four-word phrase that answers the question at the bottom of the page.

3. 
$$\log_2(75 \times 2^a) - a$$

4. 
$$\log_2 ab^5$$

5. 
$$\log_2(36 \times 2^5) - 5$$

**8.** 
$$\log_2(a \times 2^8)$$

**9.** 
$$\log_2(3a \times 2^9)$$

**10.** 
$$\log_2 2^{16} - 8$$

**11.** 
$$\log_2\left(\frac{6^2}{2a}\right) + \log_2(2a)$$

**12.** 
$$\log_2(a^4b^3)$$

13. 
$$(\log_2 75)(\log_2(2^{a+1}) - a)$$

**14.** 
$$(\log_2 2)(\log_2 ab^5)$$

15. 
$$\log_2\left(\frac{a^4}{b^3}\right)$$

**A.** 
$$\log_2 a + 5 \log_2 b$$

**B.** 
$$4 \log_2 a - 3 \log_2 b$$

$$C. -1$$

**D.** 
$$\log_2(5a) - 9$$

**E.** 
$$5 \log_2 2 + \log_2 2^{20}$$

F. 
$$log_2(3b)$$

**G.** 
$$\log_2(3a) + 9$$

1. 
$$2(\log_2 2 + \log_2 3)$$

**N.** 
$$2 \log_2 5 + \log_2 3$$

**O.** 
$$\log_2 a + 8$$

**P.** 
$$3 \log_2 3 + \log_2 4$$

$$\mathbf{R}. \ a+b$$

**S.** 
$$4 \log_2 a + 3 \log_2 b$$

## 7-4

### **Practice**

Form G

Properties of Logarithms

Write each expression as a single logarithm.

1. 
$$\log_5 4 + \log_5 3$$

**4.** 
$$5 \log_7 x = 2 \log_7 x$$

7. 
$$2 \log x - 3 \log y$$

**10.** 
$$5 \log 2 - 2 \log 2$$

13. 
$$(\log 3 - \log 4) - \log 2$$

**16.** 
$$\log 2 + \log 4 - \log 7$$

**19.** 
$$\frac{1}{2}\log x + \frac{1}{3}\log y - 2\log z$$

Expand each logarithm. Simplify if possible.

**24.** 
$$\log 6x^3 y$$

**25.** 
$$\log 7(3x-2)^2$$

**27.** 
$$\log \frac{5x}{4y}$$

**28.** 
$$\log_5 5x^{-5}$$

**30.** 
$$\log_4 (3xyz)^2$$

Use the Change of Base Formula to evaluate each expression. Round your answer to the nearest thousandth.

**39.** The concentration of hydrogen ions in a batch of homemade ketchup is  $10^{-4}$ . What is the pH level of the ketchup?